

# Stochastic cloud generator for McICA radiation calculations

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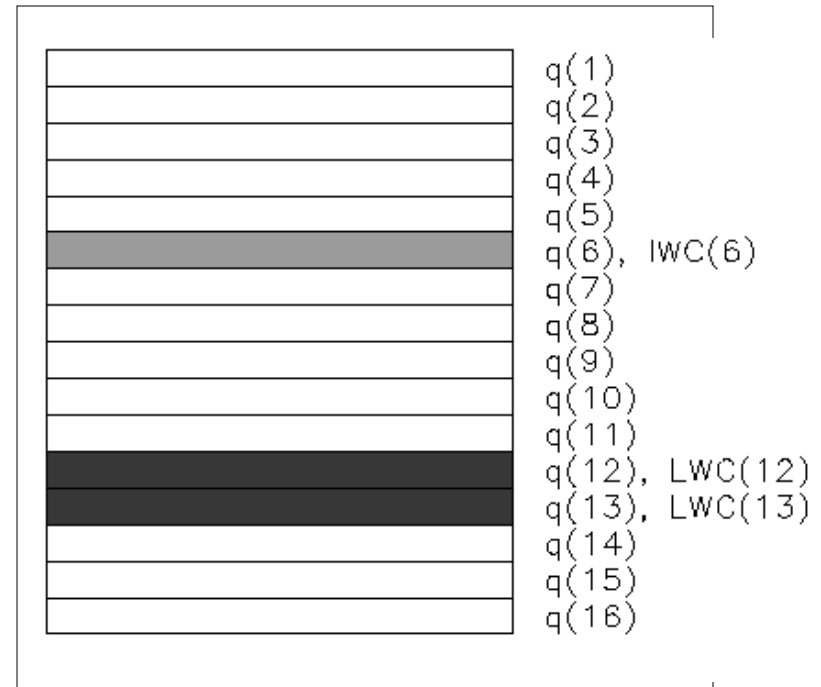


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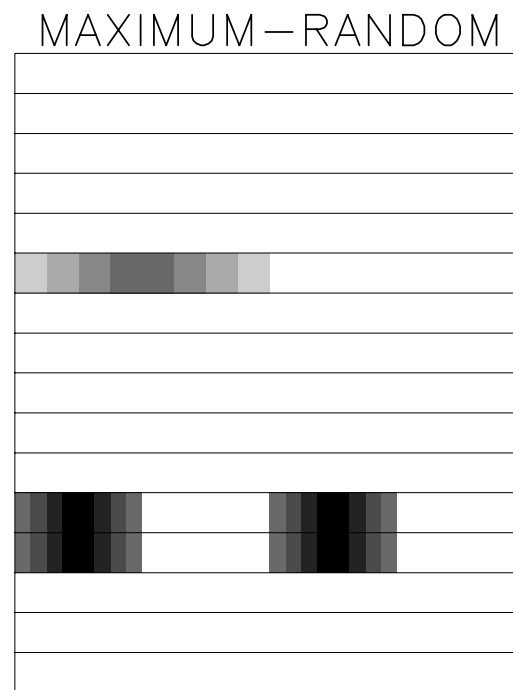
# 1. Motivation

- Large-scale atmospheric models (LSAMs) use 1D radiation schemes
- In its basic form, a 1D radiation code computes radiative fluxes and heating rates for a plane-parallel horizontally homogeneous (pph) column, given the vertical profile of H<sub>2</sub>O and other trace gases, cloud water etc.
- However, the atmosphere is not horizontally homogeneous at the scale of LSAM grid cells

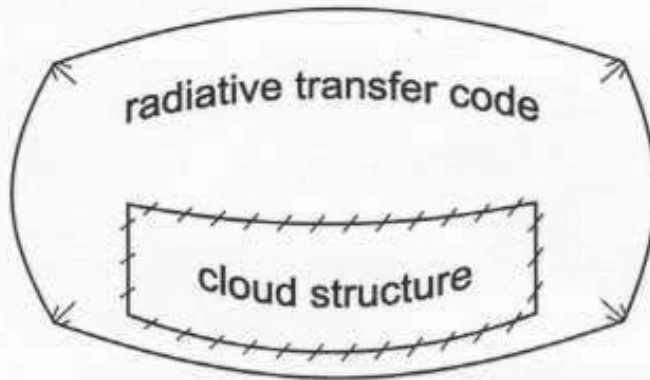


## Treatment of subgrid-scale clouds: conventional approach

- Assumptions about cloud horizontal variability and cloud overlap built in the radiation code.
- E.g.: Oreopoulos and Barker (1999): attempt to combine gamma-weighted two-stream approximation with maximum-random overlap of clouds.
- Result: complex 1D radiation codes that are difficult to modify – even if the assumptions about subgrid-scale cloud structure are known to be biased!



Existing paradigm:

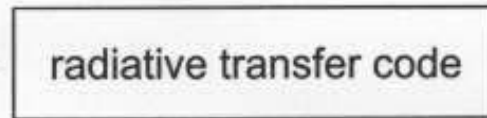


biased

radiative fluxes

Alternate view:

cloud structure



unbiased

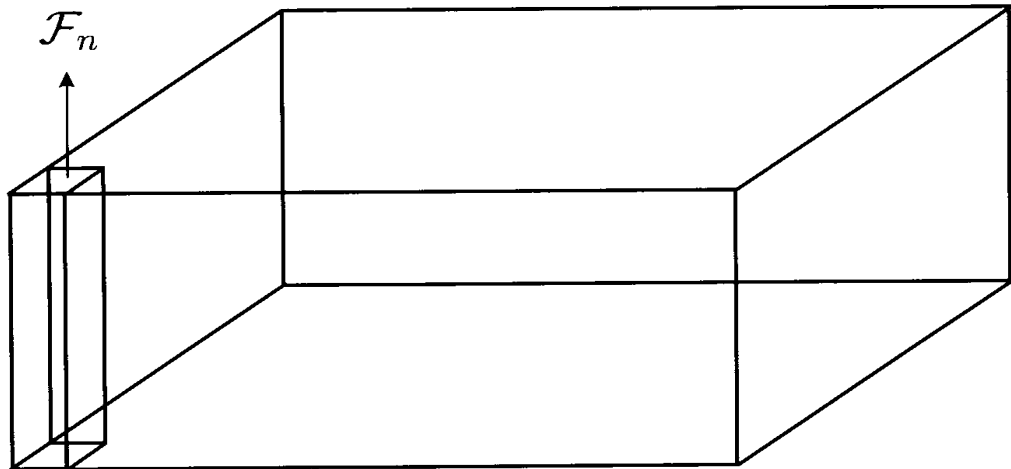
- much more desirable configuration
- essential if subtle effects and cloud/radiative feedbacks are to be captured

## 2. (a) ICA = Independent Column Approximation

- ICA allows to separate subgrid-scale cloud structure from the radiation code!
- Assume zero net horizontal radiative transport (a good assumption when computing domain-average flux profiles).
- Perform the radiation calculations separately for the  $N$  independent columns

=> domain average

$$\langle F \rangle_{\text{ICA}} = \frac{1}{N} \sum_{n=1}^N F_n$$



## 2(b). McICA = Monte Carlo Independent Column approximation

Most GCM-type radiation codes use the k distribution method for gas absorption

=> in effect, the spectrum is divided into  $K$  parts ( $K \sim 50-100$ )

$$\Rightarrow F = \sum_{k=1}^K w_k F_k$$

When using ICA,  $\langle F \rangle_{ICA} = \frac{1}{N} \sum_{n=1}^N \sum_{k=1}^K w_k F_{n,k}$

In McICA this is approximated as  $\langle F \rangle_{McICA} = \sum_{k=1}^K w_k F_{\{\text{random}\},k}$

where  $F_{\{\text{random}\},k}$  is the radiative flux for  $k$  term  $k$  for a randomly selected subcolumn

## Properties of McICA

- Much faster than ICA. In fact, as fast (or faster than) present 1D radiation codes
- Unbiased with respect to ICA.
- Significant random errors. Does this matter?
  - \* A non-trivial question
  - \* Errors are spatially and temporally localized
  - \* GCM estimates of large-scale variables are not perfect
  - \* There is no one-to-one correlation between large-scale variables and (large-scale) radiative fluxes
  - \* Random errors can be reduced by doing more than one loop over the  $k$  distribution

### 3. Stochastic cloud generator

Unless a super parameterization (2D CRM for each GCM grid cell) is used, the columns needed by McICA have to be generated using model large-scale variables. A simple stochastic cloud generator was developed for that purpose.

#### GENERATION OF CLOUD FRACTION

Define a variable  $x \in [0,1]$  (“cumulative frequency”) such that

$$\begin{cases} x_j \leq 1 - C_j \Leftrightarrow \text{layer } j \text{ clear for this subcolumn} \\ x_j > 1 - C_j \Leftrightarrow \text{layer } j \text{ cloudy for this subcolumn} \end{cases}$$

The algorithm for generating  $x$  depends on cloud overlap assumptions. For example,

$$\begin{cases} x_j = \text{RND} \Leftrightarrow \text{random overlap} \\ x_j = x_{j-1} \Leftrightarrow \text{maximum overlap} \end{cases}$$

## Preferred approach: generalized cloud overlap

(Hogan & Illingworth, 2000)

Total cloud fraction for clouds in layers  $j$  and  $k$

$$C_{jk} = \alpha_{jk} C_{jk,\max} + (1 - \alpha_{jk}) C_{jk,\text{ran}}$$

$$C_{jk,\max} = \max(C_j, C_k)$$

$$C_{jk,\text{ran}} = C_j + C_k - C_j C_k$$

This can be generated stochastically, subject to two assumptions:

- (a) The true overlap is between random and maximum  $(0 \leq \alpha \leq 1)$
- (b) It is sufficient to consider parameter  $\alpha$  for adjacent layers

$$\alpha_{jk} = \alpha_{j,j+1} \times \alpha_{j+1,j+2} \times \dots \times \alpha_{k-1,k}$$

- This is consistent with the decorrelation depth ( $L_c$ ) approach by Bergman and Rasch (2002):

$$\alpha_{jk} = \exp[-(z_j - z_k) / L_c]$$

## Resulting algorithm for generating the profile of $x$

Uppermost layer ( $j = 1$ ):

$$x_1 = \text{RND}$$

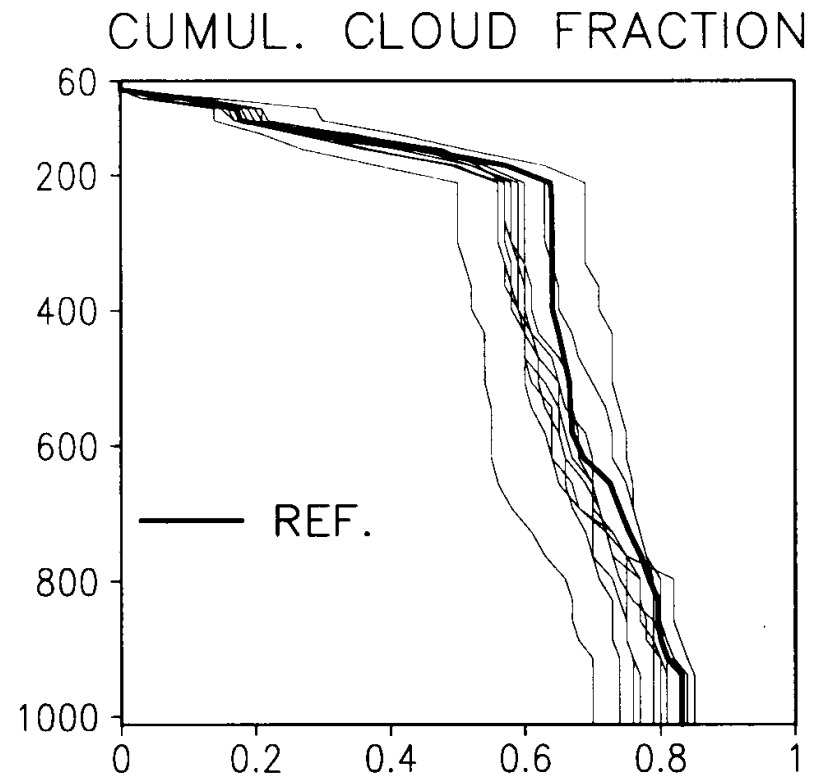
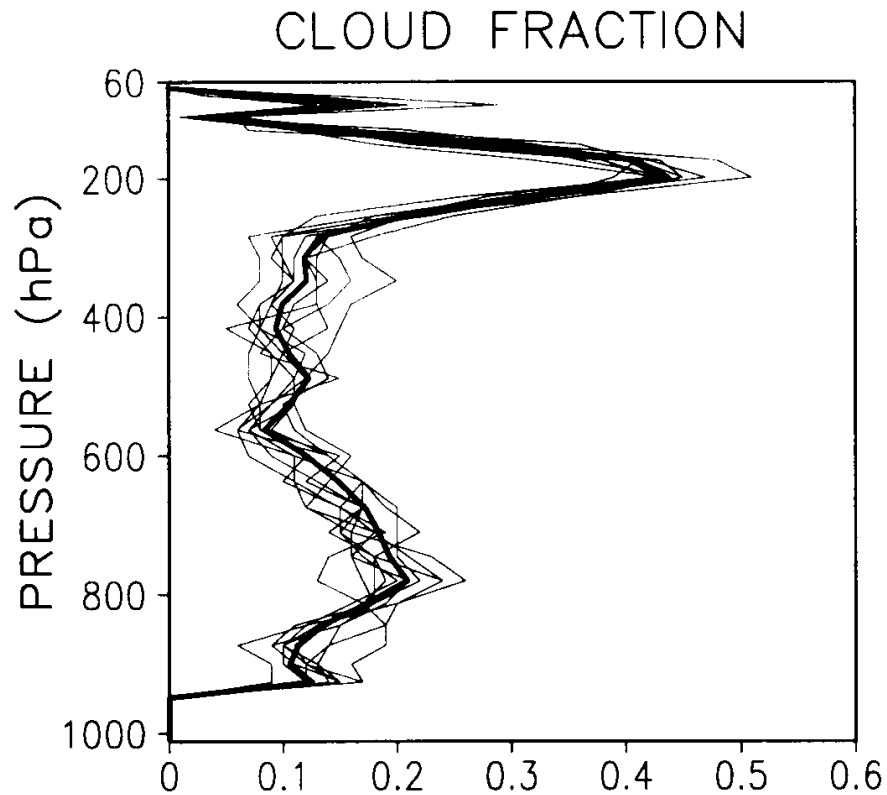
Other layers ( $j > 1$ ):

$$\begin{cases} \text{RND}_1 < \alpha_{j-1,j} \Rightarrow x_j = x_{j-1} \text{ (maximum overlap)} \\ \text{RND}_1 \geq \alpha_{j-1,j} \Rightarrow x_j = \text{RND}_2 \text{ (random overlap)} \end{cases}$$

$\text{RND}$ ,  $\text{RND}_1$  and  $\text{RND}_2$  are random numbers  $\in [0,1]$

## EXAMPLE

Ten samples for a cloud fraction profile from a tropical squall line CRM simulation (simulated area mean layer cloud fraction and cumulative cloud fraction, 100 subcolumns per sample)



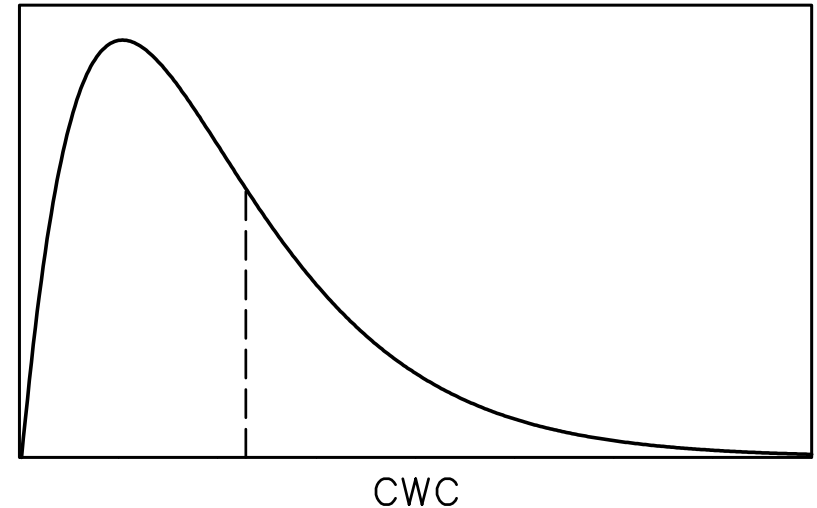
# Generation of cloud water content (CWC)

- Assumption: cumulative frequency for cloud fraction ( $x$ ) can also be used for that:

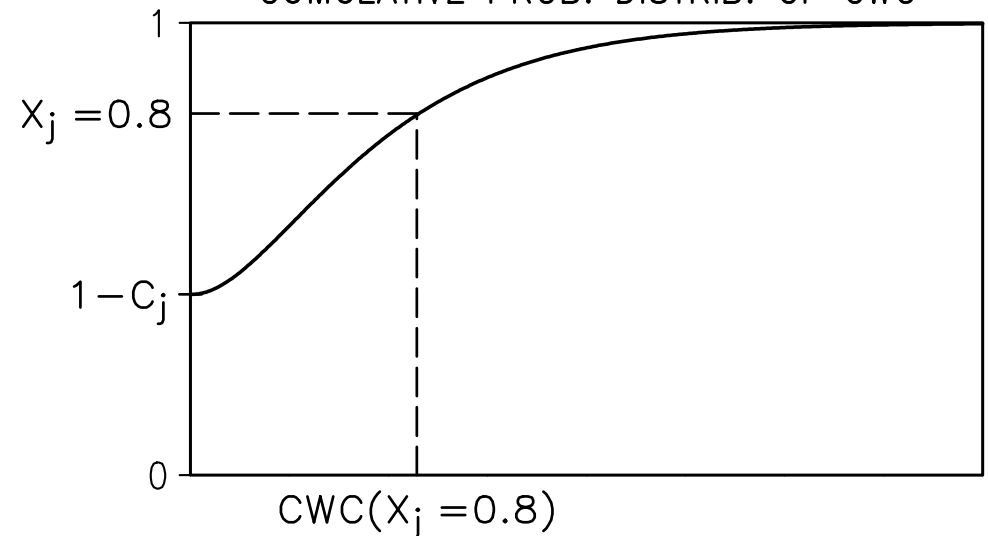
$$x_j = 1 - C_j \Rightarrow \text{smallest CWC}$$
$$x_j = 1 \quad \Rightarrow \text{largest CWC}$$

- Mean value and standard deviation of CWC from host model (here: CRM data)
- In principle, any form can be assumed for the probability distribution of CWC ( $\beta$  and  $\gamma$  distributions implemented)

PROB. DISTRIB. OF CWC (CLOUDY PART)



CUMULATIVE PROB. DISTRIB. OF CWC



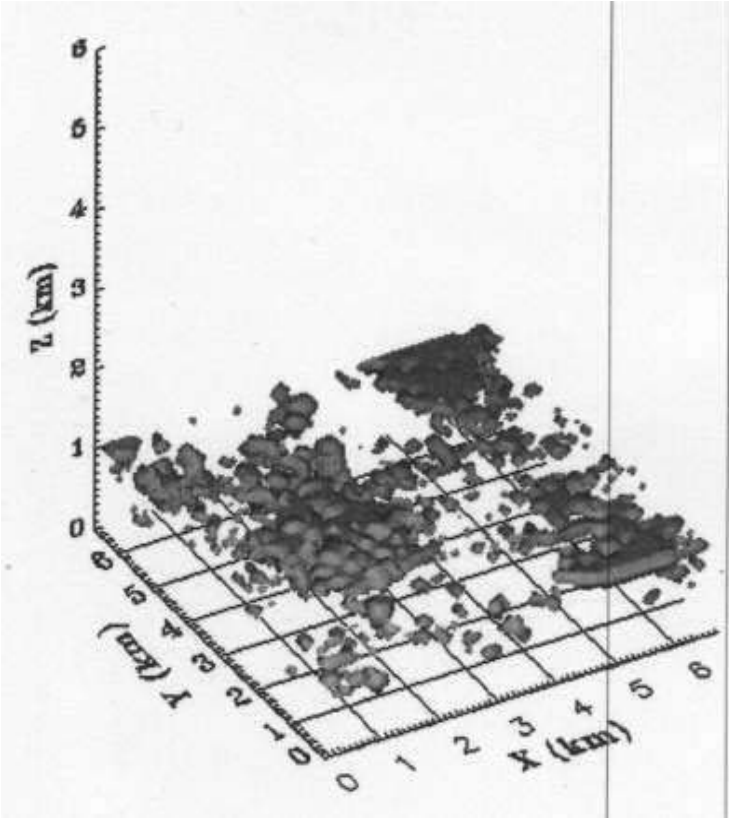
## 4. Cloud data

- Cloud condensate fields taken from 3D cloud-resolving model (CRM) simulations
- Boundary layer clouds: ATEX, BOMEX
- Vigorous shallow convection: OPEN CELLS
- Deep tropical convection: GATE\_A, GATE\_B  
GATE\_A-liq, GATE\_B-liq

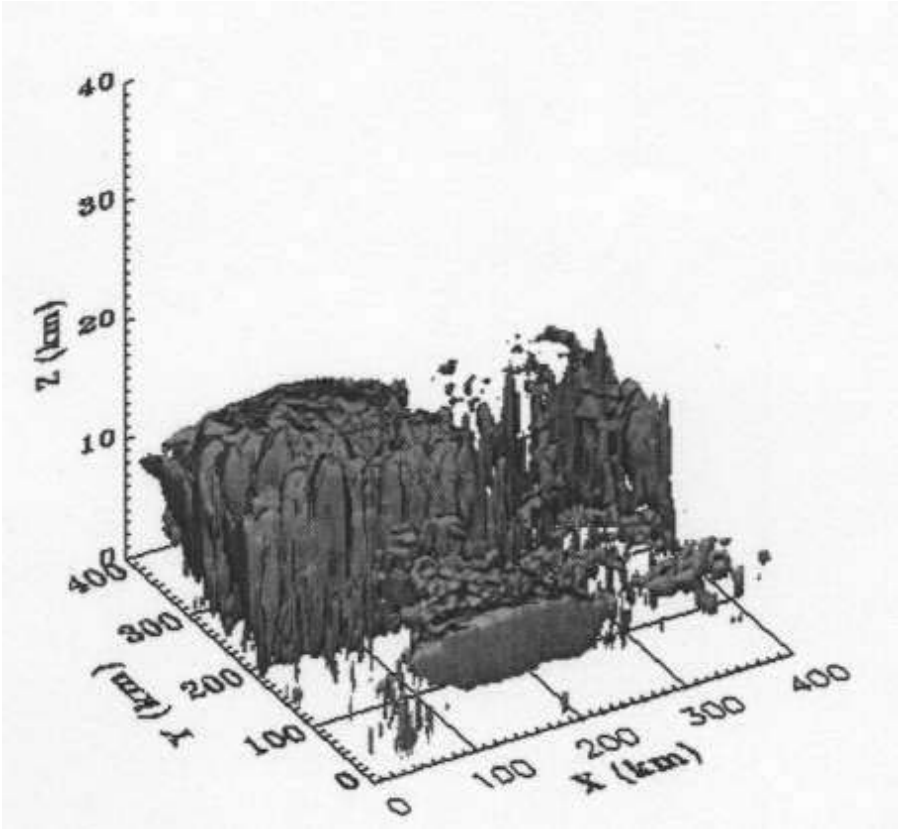
## Cloud field statistics

	$\Delta L$ (km)	$C_{\text{tot}}$	$\bar{\tau}$	$\sigma_{\tau} / \bar{\tau}$
ATEX	6.8	0.565	15.3	1.49
BOMEX	6.4	0.150	6.3	1.63
OPEN CELLS	50	0.903	55.8	1.38
GATE A	400	0.996	54.9	1.95
GATE B	400	0.999	40.2	2.32
GATE A-liq	400	0.462	62.7	1.99
GATE B-liq	400	0.251	67.1	2.21

# ATEX



# GATE B



## 5. Radiation code

- CCC radiation code by Jiagnan Li
- 31  $k$  terms in the SW and 46  $k$  terms in the LW region

### Input for radiation calculations

From CRM data: Cloud fraction

mean LWC, IWC and CWC (=LWC+IWC)

std. dev. of CWC

overlap parameter  $\alpha$

Assumed: fixed effective size for water droplets and ice crystals

$$(r_e = 9.9 \mu\text{m}, D_{ge} = 50 \mu\text{m})$$

surface albedo = 0.1, solar zenith angle = 60 deg

## 6. Results

### Two sources of error

- (a) Cloud generator: not able to simulate cloud field structure perfectly => biases
  
- (b) McICA: incomplete sampling of the cloud field  
=> random errors

## 6(a). Errors due to the cloud generator

Reference: ICA calculations with original CRM data

Compute errors for McICA with a very large number of columns from the stochastic cloud generator (620 000 for SW, 920 000 for LW) => sampling errors  $\rightarrow 0$ .

=> denoted as “**Stoch\_20000**”

For comparison, compute errors for

MRO\_pph – maximum random overlap, plane-parallel horizontally homogeneous (pph) clouds

MRO\_var – maximum random overlap, cloud horizontal variations included

RAN\_pph – random overlap, pph clouds

RAN\_var – random overlap, horizontally variable clouds

## Errors in total cloud fraction

	Stoch_20000	MRO	RAN
ATEX	0.002	-0.067	0.015
BOMEX	0.000	-0.032	0.033
OPEN CELLS	-0.011	-0.216	0.097
GATE A	-0.002	-0.079	0.004
GATE B	-0.001	-0.019	0.001
GATE A-liq	0.025	-0.265	0.365
GATE B-liq	0.026	-0.170	0.358

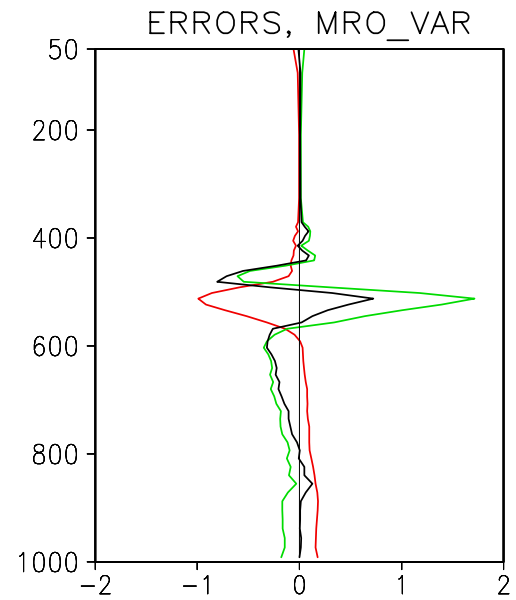
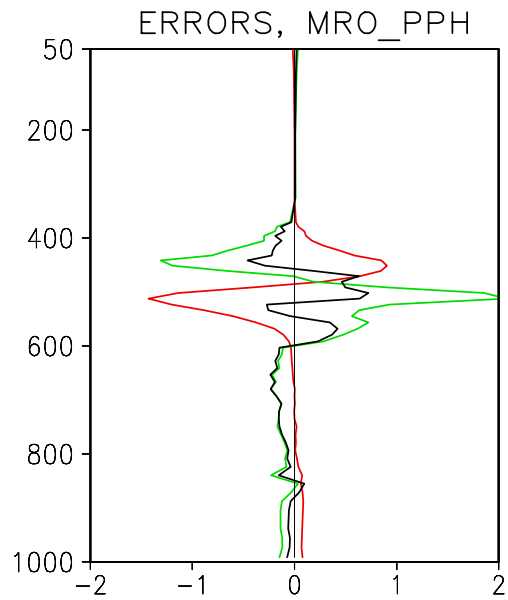
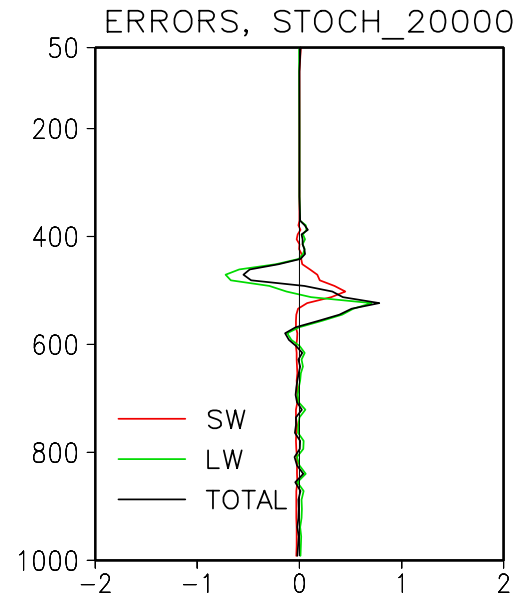
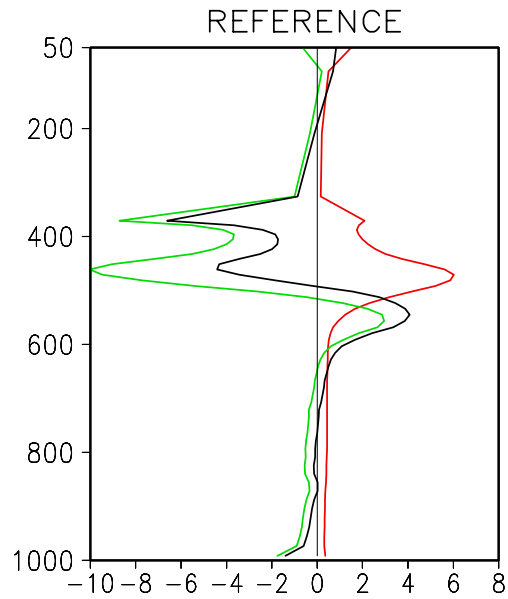
Upward SW flux at the TOA ( $\text{W m}^{-2}$ )  
 (reference values and errors)

	Ref.	Stoch _20000	MRO _pph	MRO _var	RAN _pph	RAN _var
ALEX	204.1	-2.8	28.3	-21.6	44.4	-0.3
BOMEX	113.8	-0.4	2.8	-4.4	10.5	4.2
OPEN CELLS	388.5	9.9	-26.1	-64.8	99.3	94.8
GATE A	354.2	7.4	18.6	-90.2	118.3	101.8
GATE B	350.1	3.8	67.7	-77.6	112.4	93.2
GATE A-liq	208.3	17.0	-41.4	-58.0	147.1	114.7
GATE B-liq	152.1	12.6	-29.2	-35.3	117.8	93.9

Outgoing LW radiation ( $\text{W m}^{-2}$ )  
 (reference values and errors)

	Ref.	Stoch _20000	MRO _pph	MRO _var	RAN _pph	RAN _var
ALEX	326.8	0.3	-1.0	1.0	-1.8	0.2
BOMEX	340.8	0.0	-0.1	0.2	-0.5	-0.2
OPEN CELLS	188.4	-0.8	8.7	11.5	-16.6	-15.1
GATE A	178.2	6.3	-4.9	25.9	-16.9	-9.6
GATE B	168.9	16.1	-16.9	36.1	-20.6	-5.4
GATE A-liq	261.4	-0.2	3.4	4.1	-11.6	-9.3
GATE B-liq	270.5	-0.3	1.9	2.2	-9.6	-7.9

# HEATING RATES FOR OPEN CELLS (K/d)



## 6(b). Sampling errors

Reference: McICA calculations with a very large number of columns from the stochastic cloud generator (“**Stoch\_20000**”)

Make a sample of 2000 calculations so that there is only one loop over the  $k$  distribution (i.e., one subcolumn per  $k$  term) (“**Stoch\_1**”).

Compute error statistics compared to **Stoch\_20000**.

RMS sampling errors for **Stoch\_1** (W m<sup>-2</sup> or K day<sup>-1</sup>)

	$F_{SW}^{\uparrow}$	$F_{LW}^{\uparrow}$	$(\partial T / \partial t)_{SW}$	$(\partial T / \partial t)_{LW}$
ATEX	73.9	3.3	0.59	0.88
OPEN_CELLS	72.9	10.4	1.18	2.15
GATE B	73.6	14.8	0.98	1.14
GATE B-liq	76.3	6.9	0.61	0.89

## Reduction of sampling errors:

### Trick 1: Use only cloudy columns for McICA

Estimate all-sky fluxes as

$$F_{\text{all}} = C_{\text{tot}} F_{\text{cloudy}} + (1 - C_{\text{tot}}) F_{\text{clear}}$$

This is not expensive because

- Clear-sky fluxes  $F_{\text{clear}}$  are computed for diagnostics
- Total cloud fraction  $C_{\text{tot}}$  can be estimated rapidly using the cloud generator (here, 300 columns used for that)

These results are denoted as “**Stoch\_1\***”

RMS sampling errors for **Stoch\_1\*** (W m<sup>-2</sup> or K day<sup>-1</sup>)

(relative differences to (%) **Stoch\_1** in blue.)

	$F_{SW}^{\uparrow}$	$F_{LW}^{\uparrow}$	$(\partial T / \partial t)_{SW}$	$(\partial T / \partial t)_{LW}$
ATEX	39.5 (-47)	1.5 (-55)	0.39 (-34)	0.54 (-38)
OPEN_CELLS	46.1 (-37)	4.6 (-56)	1.09 (-8)	1.95 (-9)
GATE B	74.3 ( 1)	14.7 (-1)	0.96 (-2)	1.13 (-1)
GATE B-liq	20.5 (-73)	2.7 (-61)	0.32 (-48)	0.45 (-49)

## Reduction of sampling errors:

### Trick 2: Improved spectral sampling

The best strategy is not to use equally many subcolumns for every k term but to add the extra subcolumns for those k terms that are associated with large cloud radiative effects.

Test: Use 50% more subcolumns (47 in the SW, 69 in the LW)  
(and include Trick 1: only cloudy columns for McICA)

=> **Stoch\_1.5\***

RMS sampling errors for **Stoch\_1.5\*** (W m<sup>-2</sup> or K day<sup>-1</sup>)

(relative differences (%) to **Stoch\_1\*** in red  
and to **Stoch\_1** in blue.)

	$F_{SW}^{\uparrow}$	$F_{LW}^{\uparrow}$	$(\partial T / \partial t)_{SW}$	$(\partial T / \partial t)_{LW}$
ATEX	18.1 (-54 / -76)	0.7 (-53 / -79)	0.16 (-57 / -72)	0.20 (-63 / -77)
OPEN_CELLS	20.8 (-55 / -71)	2.1 (-54 / -80)	0.58 (-46 / -51)	0.99 (-49 / -54)
GATE B	32.4 (-56 / -56)	6.1 (-59 / -59)	0.48 (-50 / -51)	0.59 (-47 / -48)
GATE B-liq	10.7 (-48 / -86)	1.2 (-56 / -83)	0.14 (-55 / -77)	0.19 (-58 / -78)

## 7. Conclusions

- A simple stochastic cloud generator has been developed for use in McICA radiation calculations
- Systematic errors in cloud cover, radiative fluxes and heating rates are significantly smaller than for traditional cloud overlap assumptions
- Random errors can be reduced substantially by improved sampling of the cloud field and improved spectral sampling

# HEATING RATES FOR GATE\_B (K/d)

